

Lecture program



https://moodle2.hs-kempten.de/moodle/course/view.php?id=2914

Nr.	Datum	Inhalt	Ort	Von Wem
1	01.10.	Virtual Test Driving (VTD) CarMaker Quick Start Guide	T314	Self-study
2	08.10.	Requirements for vehicles and their global attributes	T314 Zoom	Schick
3	15.10.	Vehicle dynamics attributes and their target conflicts	T314 Zoom	Schick
3	22.10.	Test and evaluation methods for vehicle attributes (1) with practical simulation	T314 Zoom	Schick
4	29.10.	Test and evaluation methods for vehicle attributes (2) with practical simulation	T314 Zoom	Schick
5	05.11.	ADAS DRIVING EVENT Measurement Tech. Introductions	Living Lab	Günther/Riedlmüller/ Schwandke
6	12.11.	Basic vehicle dynamics calculation and vehicle models with exercise	T314 Zoom	Schick
7	19.11.	Chassis components and functions (1) Tire & Wheels	T314 Zoom	Schick

	14	21.01.	Exam preparation	T314	Schick
7	13	14.01.	Analysis of international standards and application into the simulation	T314 Zoom	Schick
	12	07.01.	Chassis controls and functions (3) ESP-Application & Hands-On Workshop	T314 Zoom	Herr Lutz (BOSCH)
	11	17.12.	Chassis controls and functions (2) ESP–Functions & Application & Process	T314 Zoom	Herr Lutz (BOSCH)
	10	10.12.	Chassis controls and functions (1) Overview & Brakes & Steering	T314 Zoom	Schick
	9	03.12.	TEND: ADAS Development for a sports car manufacturer	T314 Zoom	Manuel Höfer (Porsche)
	8	26.11.	Chassis components and functions (2) Axle & Suspension	T314 Zoom	Schick



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What is a model?



A simplified representation of the reality.

What is a vehicle dynamics model?



Refers to calculate the dynamic motion of ground vehicles for engineering tasks.

Where do we need vehicle dynamics models?



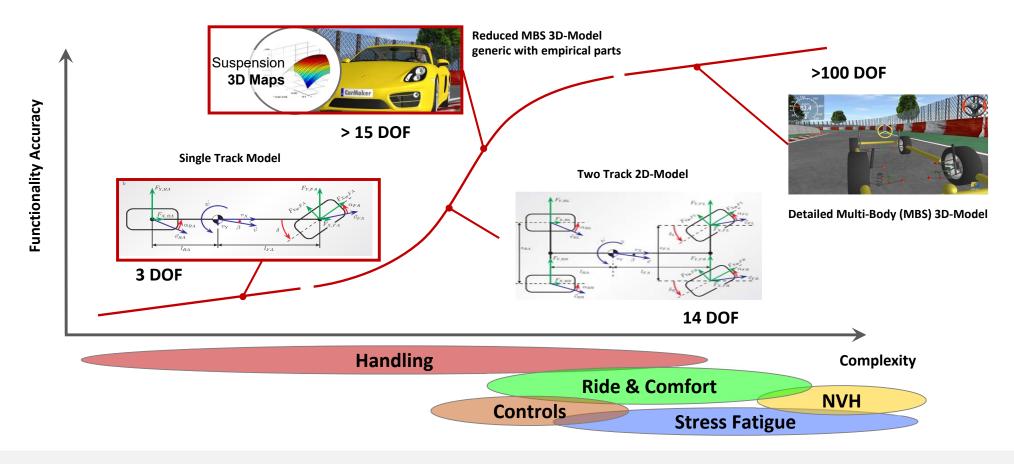
Simulation, model based testing and model based control methods.

When is a vehicle dynamics model valid?

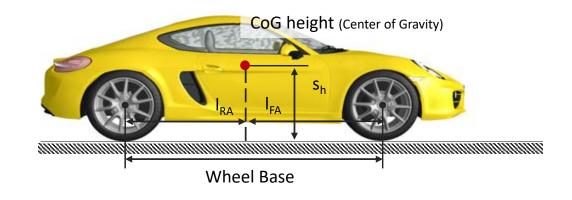


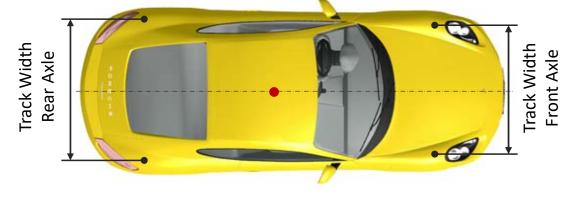
Good and accurate enough for the application purpose?

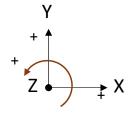
Classification an positioning of vehicle dynamics models



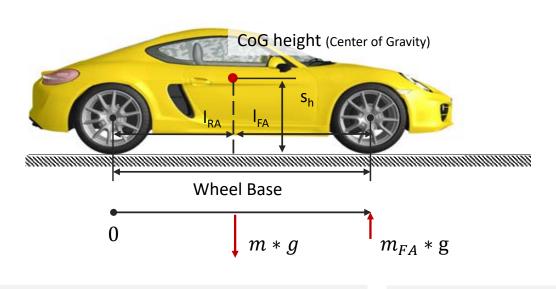
Basic chassis dimensions





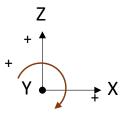


Calculation of CoG – Center of Gravity



$$m * g * l_{RA} = m_{FA} * g * l$$
 $l_{FA} = l - l_{RA}$

$$l_{FA} = l - l_{RA}$$



$$\sum F_z=0$$

- Vehicle weight (with driver) = 1.970 kgm_{FA} (front axle) = 1100 kgm_{RA} (rear axle) = 870 kgWheel base $= 2.807 \, \text{mm}$
 - Center of gravity $= 0.65 \, \text{m}$

Calculation of CoG – Center of Gravity

$$m * g * l_{RA} = m_{FA} * g * l$$

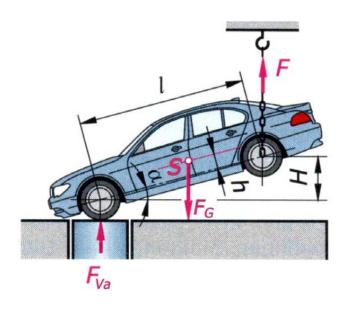
$$l_{RA} = \frac{m_{FA} * l}{m} = \frac{1100 kg * 2,807 m}{1970 kg} = 1,567 m$$

$$l_{FA} = l - l_{RA}$$

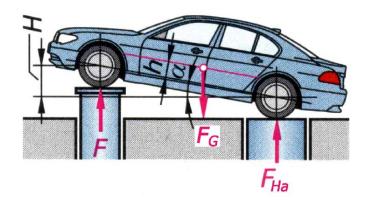
$$l_{FA} = l - l_{RA} = 2,807m - 1,567m = 1,24 m$$

Vehicle weight (with driver) = 1.970 kg
m_{FA} (front axle) = 1100 kg
m_{RA} (rear axle) = 870 kg
Wheel base = 2.807 mm,
Center of gravity = 0,65 m

Calculation of CoG – Center of Gravity



$$h = l * \frac{F_{FA} - F}{F_G * tan\alpha}$$



$$h = l * \frac{F_{HA} - F}{F_G * tan\alpha}$$

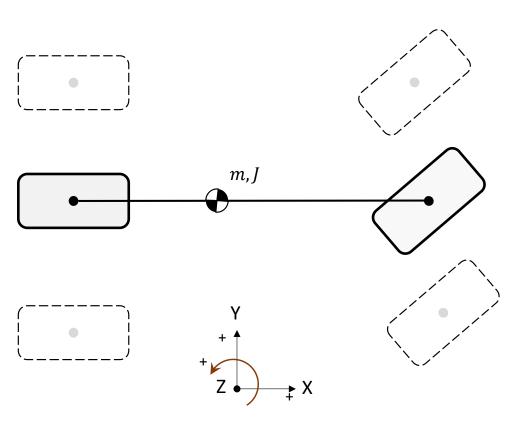
Calculation of CoG – Center of Gravity





[3]

Simplification of the vehicle model: "Single Track Model" Theory - 3 DOF



Approach

- Wheels are lumped into single track
 - → Tire side slip & axle stiffness are combined per axle
- Rigid body with CoG in-plane (on-track)
- Only horizontal movement
 - → No roll, pitch & vertical motion
- Steering angle only at the front axle

3 Degrees of Freedom (DOF)

- Longitudinal
- Lateral
- Yaw (rotation around Z)

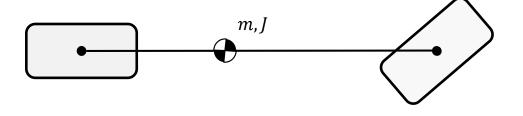
Simplification of the vehicle model: "Single Track Model" Theory - 3 DOF

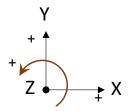
Approach

- Wheels are lumped into single track
 - → Tire side slip & axle stiffness are combined per axle



- Geometrical equation
- Equilibrium of forces & moments
- Transversal system stiffness (Tire / Axle)





3 Degrees of Freedom (DOF)

- Longitudinal
- Lateral
- Yaw (rotation around Z)

Notations

m	vehicle mass	δ	steering angle (at wheel)
F_{χ} , F_{γ}	Forces	δ_H	steering wheel angel (SWA)
F_{x_w} , F_{y_w}	Wheel forces	$i_{\scriptscriptstyle S}$	steering ratio
v	vehicle speed	ψ	yaw angle
v_x , v_y	velocity longitudinal / lateral	$\dot{\psi}$	yaw angle speed
a_x, a_y	acceleration longitudinal / lateral	R, r	course radius
	velocity front / rear axle	FA, RA	Index front axle, rear axle
l	wheel base	stat	index for stationary
l_{FA} , l_{RA}	length front / rear axle to center of gravity	CoG	center of gravity
	Side slip angle front / rear axle	EG	understeer gradient (Eigenlenkgradient)
c_{FA} , c_{RA}	side slip stiffness front / rear axle		
β	drift angle		

drift angle speed

(1)

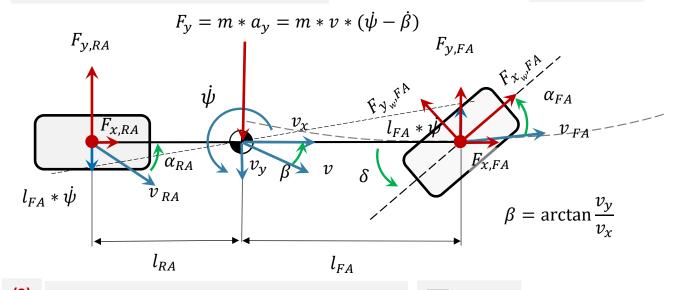
Lateral Motion
$$F_y = F_{y,FA} + F_{y,RA} = m*a_y = m*v*(\dot{\psi} - \dot{\beta})$$

 $\sum F_{y}=0$

Longitudinal Motion

$$F_{x} = F_{x,FA} + F_{x,RA} = m * a_{x}$$

$$\sum F_{x}=0$$



Rotation Z-Axle

$$\theta * \ddot{\psi} = F_{y,FA} * l_{FA} - F_{y,RA} * l_{RA}$$

$$\sum M_z = 0$$

(1)

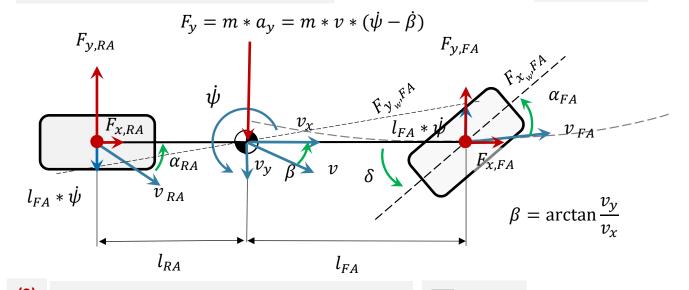
Lateral Motion
$$F_y = F_{y,FA} + F_{y,RA} = m*a_y = m*v*(\dot{\psi} - \dot{\beta})$$

 $\sum F_y = 0$

Longitudinal Motion

$$F_{x} = F_{x,FA} + F_{x,RA} = m * a_{x}$$

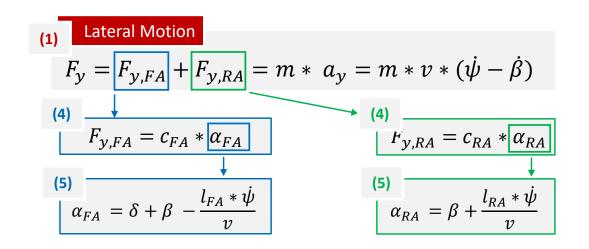
$$\sum F_{x}=0$$

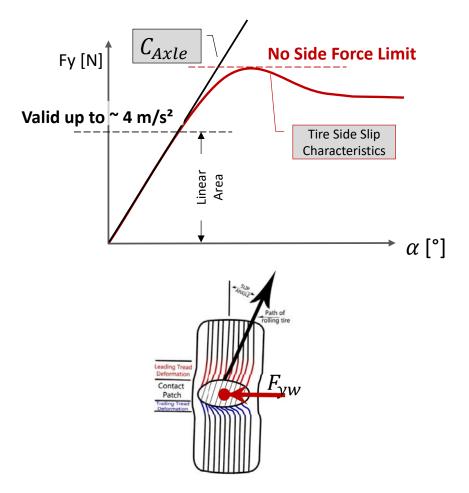


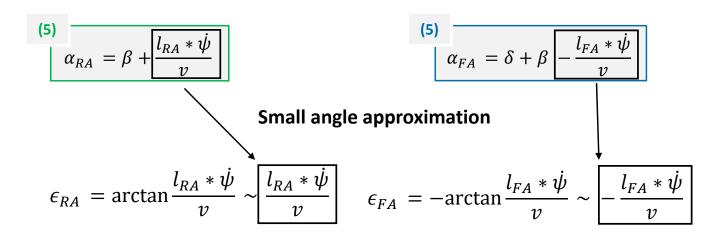
Rotation Z-Axle

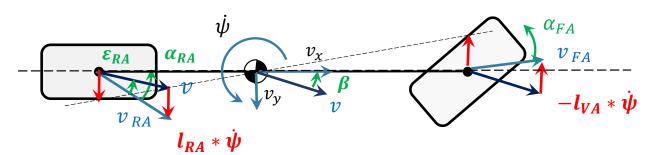
$$\theta * \ddot{\psi} = F_{y,FA} * l_{FA} - F_{y,RA} * l_{RA}$$

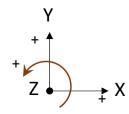
$$\sum M_z = 0$$











(9)
$$c_{FA}*\alpha_{FA}=m*\alpha_y*\frac{l_{RA}}{l}$$
 (10) $c_{RA}*\alpha_{RA}=m*\alpha_y*\frac{l_{FA}}{l}$ (11)
$$c_{FA}(\delta+\beta-\frac{l_{FA}*\dot{\psi}}{v})=m*\alpha_y*\frac{l_{RA}}{l}$$
 (12)
$$c_{RA}*(\beta+\frac{l_{RA}*\dot{\psi}}{v})=m*\alpha_y*\frac{l_{FA}}{l}$$

(13)
$$\beta = \frac{m}{l} * a_y * \frac{l_{RA}}{c_{FA}} + \frac{l_{FA} * \dot{\psi}}{v} - \delta$$

$$\beta = \frac{m}{l} * a_y * \frac{l_{FA}}{c_{RA}} - \frac{l_{RA} * \dot{\psi}}{v}$$

equalize
$$\delta = \frac{m}{l} * a_y * \frac{l_{RA}}{c_{FA}} - \frac{m}{l} * a_y * \frac{l_{VA}}{c_{RA}} + \frac{l_{FA} * \dot{\psi}}{v} + \frac{l_{RA} * \dot{\psi}}{v}$$

(16)
$$\delta = \frac{m}{l} * a_{y} * \frac{l_{RA}}{c_{FA}} - \frac{m}{l} * a_{y} * \frac{l_{VA}}{c_{RA}} + \frac{l_{FA} * \dot{\psi}}{v} + \frac{l_{RA} * \dot{\psi}}{v}$$

$$\delta = \frac{m}{l} * a_{y} * \left[\frac{l_{RA}}{c_{FA}} - \frac{l_{VA}}{c_{RA}}\right] + \frac{\dot{\psi}}{v} * \left(l_{FA} + l_{RA}\right)$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow$$

Steady-state cornering

(18)
$$\delta = \frac{l}{r} + \frac{m}{l} * \alpha_y * \left[\frac{l_{RA}}{c_{FA}} - \frac{l_{FA}}{c_{RA}} \right]$$

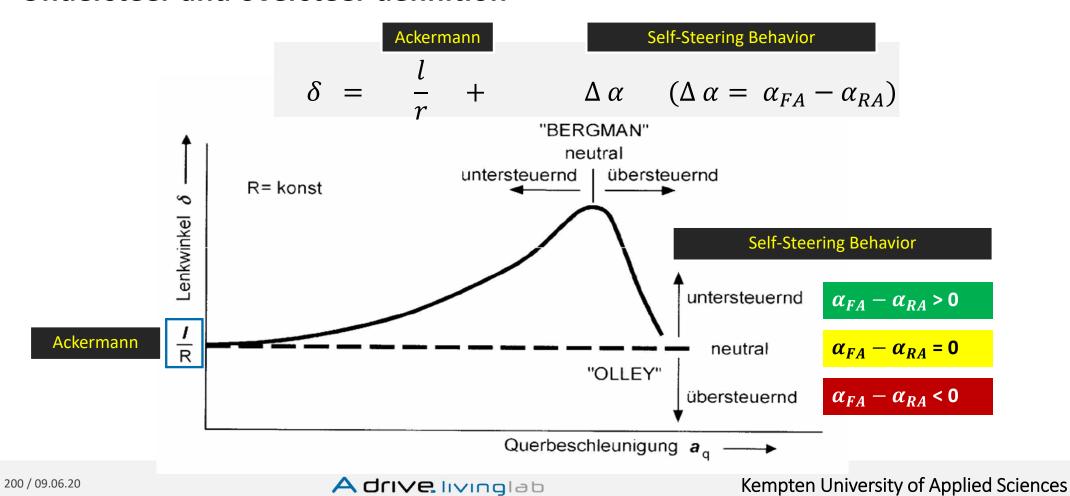
Ackermann

Self-Steering Behavior

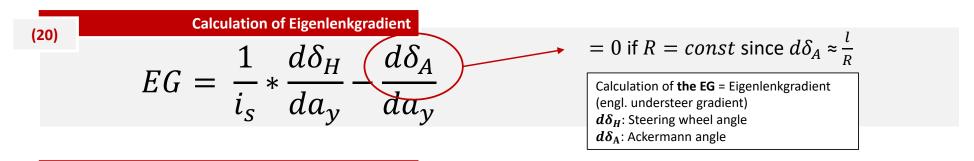
$$\Delta \alpha \quad (\Delta \alpha = \alpha_{FA} - \alpha_{RA})$$

Test and evaluation methods for vehicle attributes

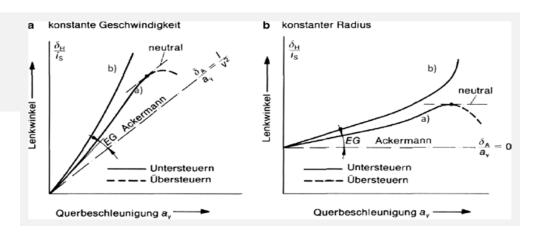
Understeer and oversteer definition



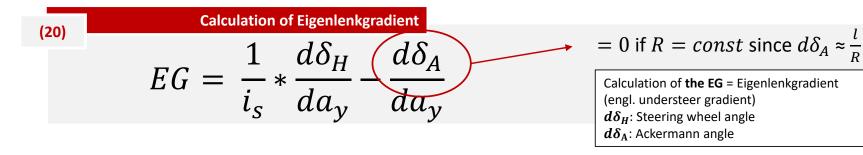
Definition of Eigenlenkgradient (Understeer Gradient)



(21) Calculation of specific Eigenlenkgradient $EG_{H} = \frac{d\delta_{H}}{da_{y}} - \frac{d\delta_{A}}{da_{y}}$ H = Hand at Steering Wheel



Definition of Eigenlenkgradient (Understeer Gradient)



(21) Calculation of specific Eigenlenkgradient $EG_{H} = \frac{d\delta_{H}}{da_{y}} - \frac{d\delta_{A}}{da_{y}}$ H = Hand at Steering Wheel

EG = 0: Neutral

EG < 0: Oversteer

EG > 0: Understeer

Characteristic Velocity and Critical Velocity

(22)

Calculation of Characteristic Velocity

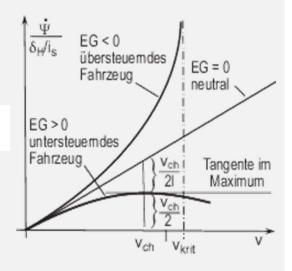
$$\left[\frac{\dot{\psi}}{\delta_H}\right]_{v_{char}} = \frac{1}{2} * \left[\frac{\dot{\psi}}{\delta_H}\right]_{EG=0} \text{ if } \frac{\dot{\psi}}{\delta_H} > \left[\frac{\dot{\psi}}{\delta_H}\right]_{EG=0} \text{ and } R = const \\ \text{i.e. if vehicle shows steady-state understeer}$$

(23)

Calculation of Critical Velocity

$$\left[\frac{\dot{\psi}}{\delta_H}\right]_{v_{crit}} = \frac{1}{2} * \left[\frac{\dot{\psi}}{\delta_H}\right]_{EG=0} \text{ if } \frac{\dot{\psi}}{\delta_H} < \left[\frac{\dot{\psi}}{\delta_H}\right]_{EG=0} \text{ and } R = const \\ \text{i.e. if vehicle shows steady-state oversteer}$$

if
$$\frac{\dot{\psi}}{\delta_H} < \left[\frac{\dot{\psi}}{\delta_H}\right]_{EG=0}$$
 and $R = const$



Practice Session: 15 min

Vehicle Dynamics in context of Advanced Driver Assistance Systems and Automated Driving



You have a vehicle with following data:

- m=1600 kg
- Wheel base = 2540 mm, Track width = 1420 mm,
- mFA = 880 kg, mRA = 720 kg,
- Steering ratio = 1:15,
- Yaw interia moment = 2800 kg m²,
- Side slip stiffness front/rear = 3000 N/°
- 1. Please calculate the center of gravity (GoG) in X-direction.
- 2. Please calculate Ackermann angle for a circle of R=100 m.
- 3. Calculate the Eigenlenkgradient (understeer gradient) between 0 4 m/s2.

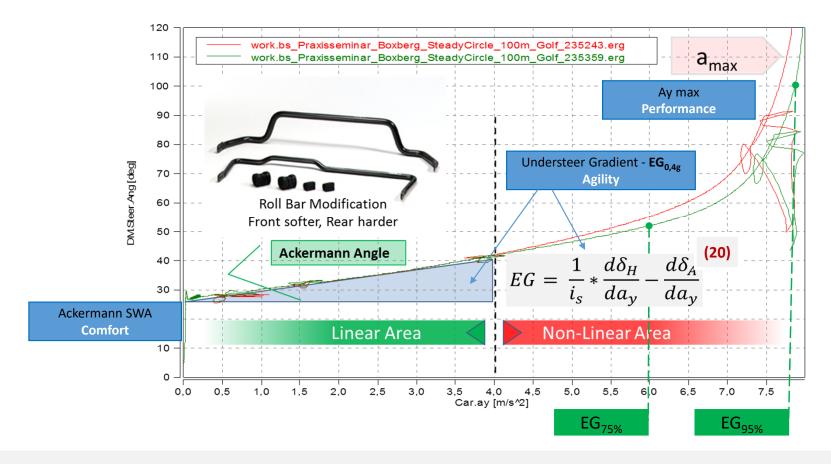
Practice Session: 15 min

- 5. How big is the steering angle for the driver at 4 m/s2?
- 6. Which measures do you recommend to reduce the understeer gradient to appr.

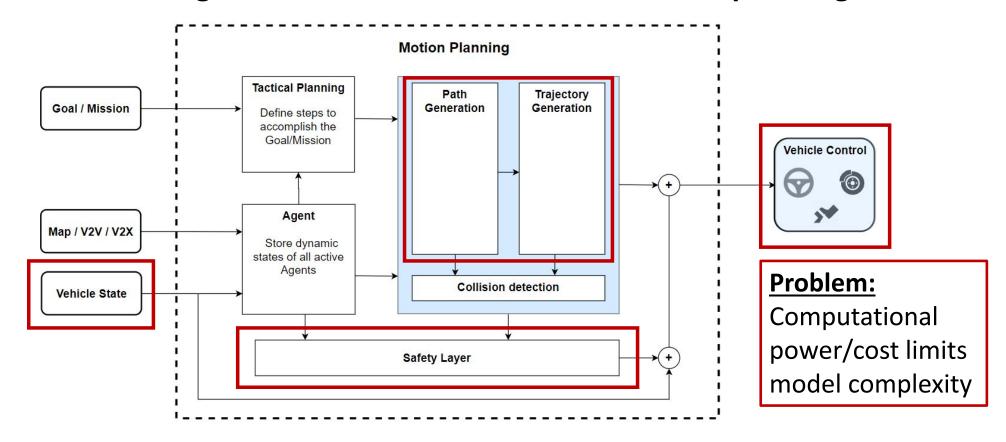
50%? Please describe 3

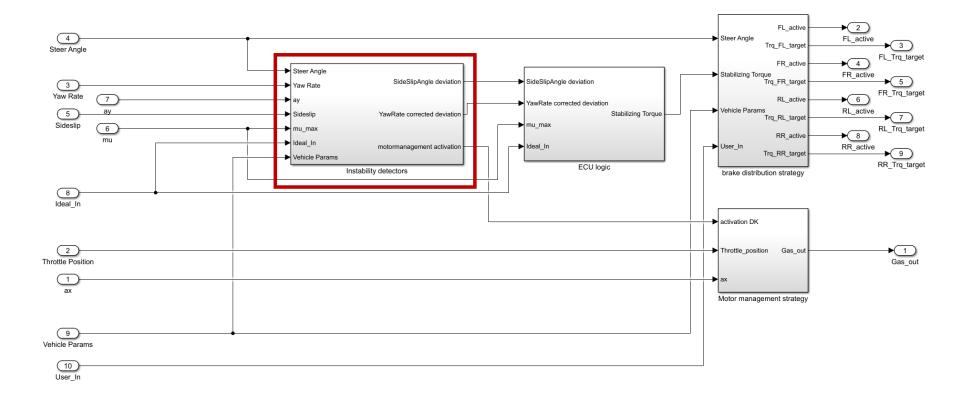
Test and evaluation methods for vehicle attributes

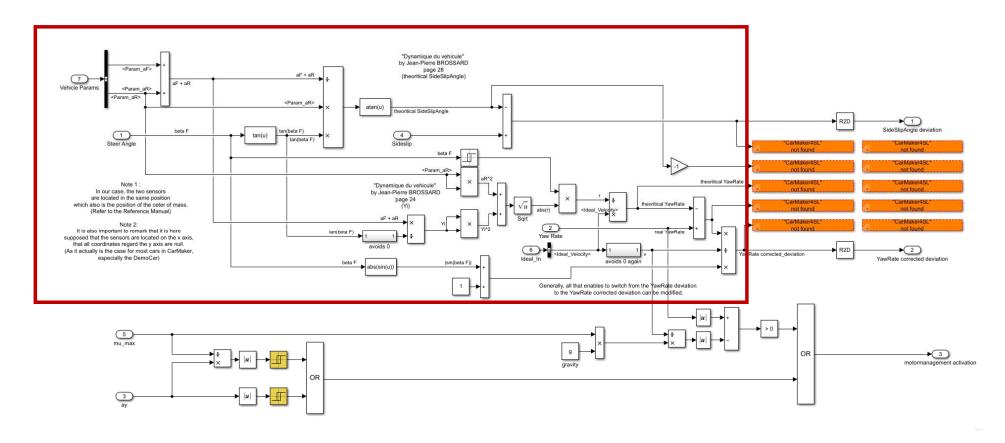
Model behavior in steady-state cornering

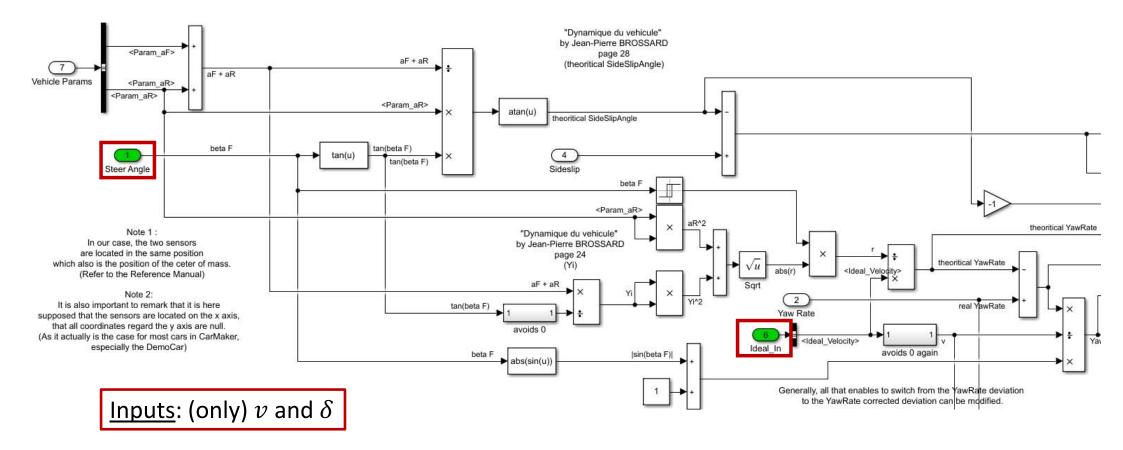


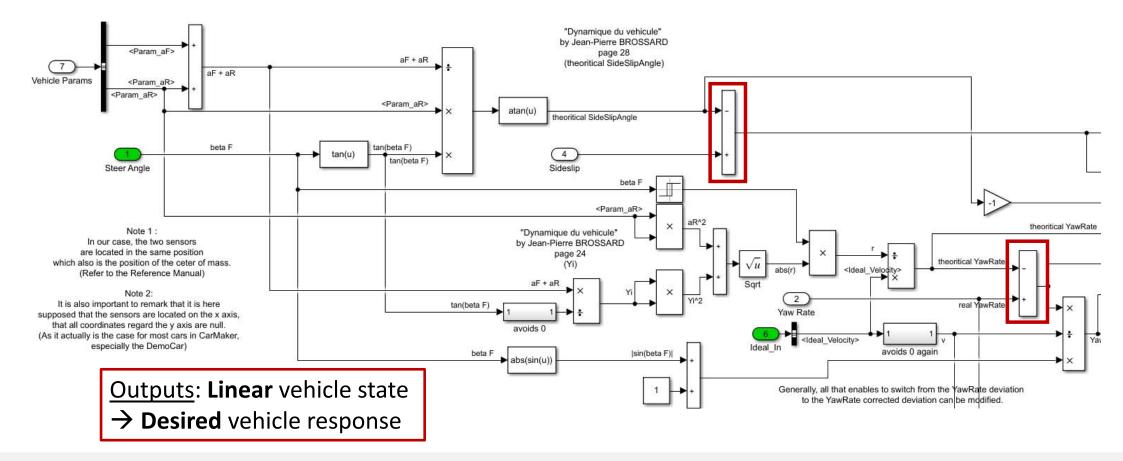
Use-Cases for a Single-track model – Model-based motion planning



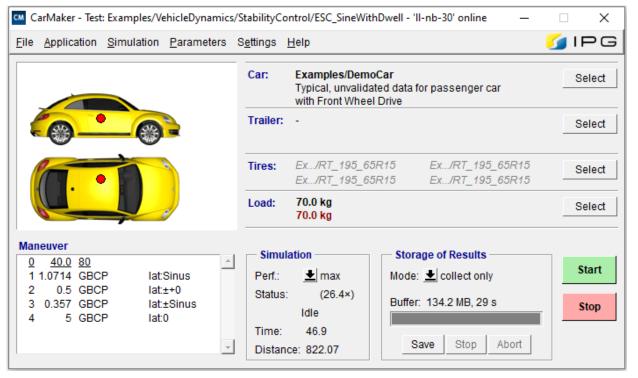


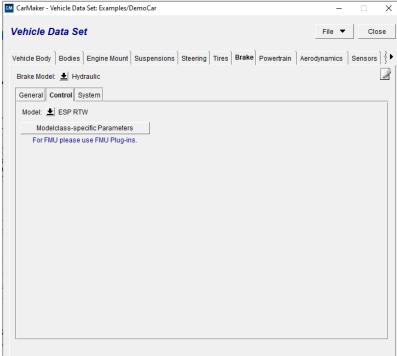




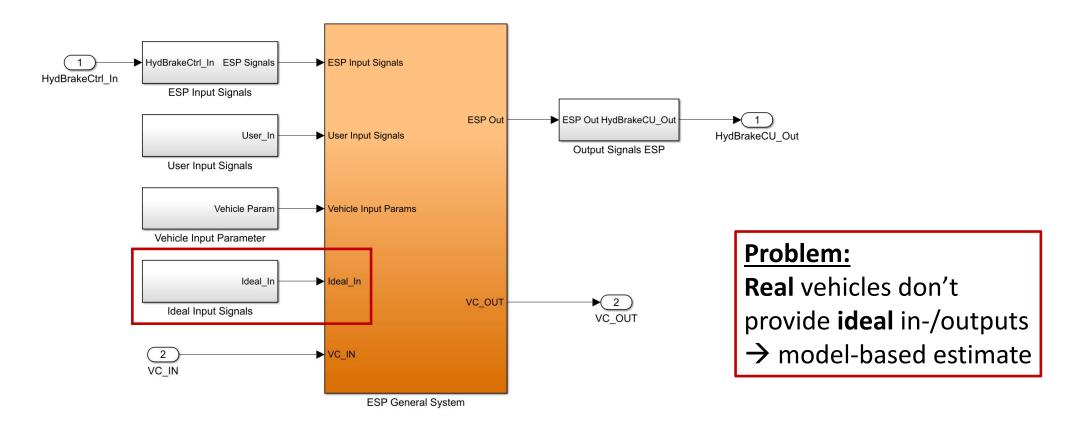


Model-based control – CarMaker example





Use-Cases for a Single-track model – Vehicle state estimation



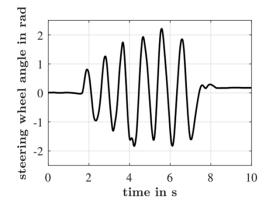
Use-Cases for a Single-track model – Vehicle state estimation

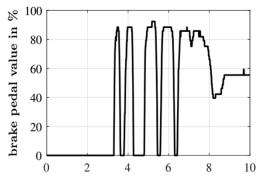
Estimation of non-measurable quantities

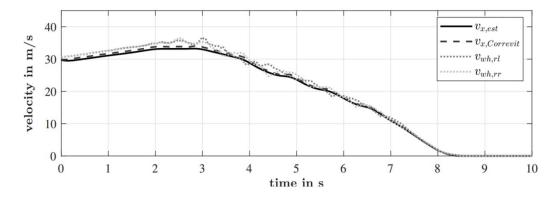
- Longitudinal velocity under slip
- Lateral velocity
- Tire forces
- Available friction coefficient (tire potential)
- Road bank angle
- ...

Prediction of vehicle state

- Motion planning
- Advanced control







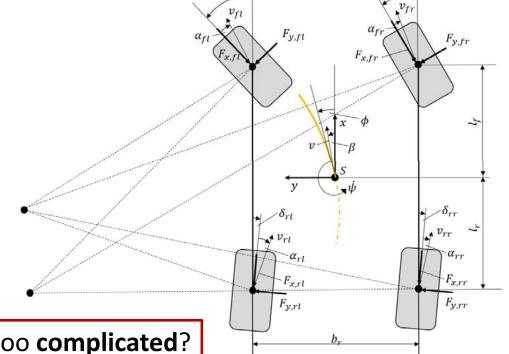
What can we improve? – Extensions of the Single-Track model

Two-track model (6 DOF)

- Consider roll, heave and pitch motion
 - → CoG height is now relevant
 - → Four wheels with **dynamic wheel load transfer**

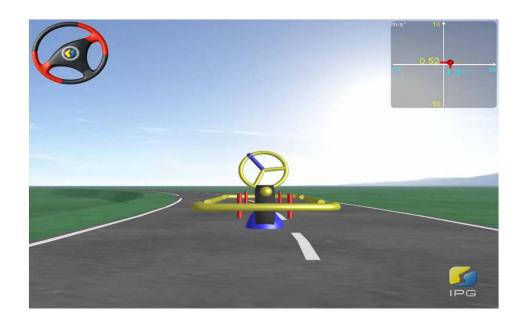
Non-linear tire modeling

- Saturation through long./lat. force limits (tire potential)
- Steering angle on both axles
- Slip-angle contribution of resulting axle stiffness
- Transient vertical dynamics
- Combined slip modeling
- ...

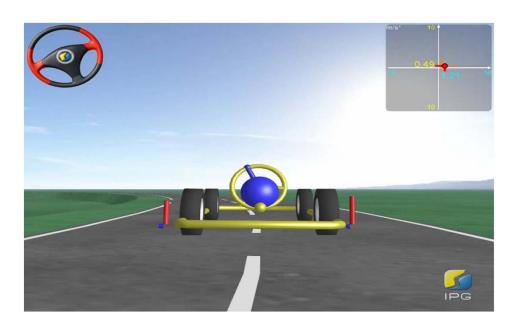


→ How **complex** is too **complicated**?

Comparison Single Track Model with 3D-MBS Model in circular driving



Single Track Model (linear)



Reduced MBS 3D-Model with empirical parts

Validity of a single-track model: CarMaker exercise

